



HAL
open science

Attractive and repulsive cracks in a heterogeneous material

Pierre-Philippe Cortet, Guillaume Huillard, Loïc Vanel, Sergio Ciliberto

► **To cite this version:**

Pierre-Philippe Cortet, Guillaume Huillard, Loïc Vanel, Sergio Ciliberto. Attractive and repulsive cracks in a heterogeneous material. 2008. ensl-00299089v1

HAL Id: ensl-00299089

<https://ens-lyon.hal.science/ensl-00299089v1>

Preprint submitted on 17 Jul 2008 (v1), last revised 13 Mar 2018 (v2)

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Attractive and repulsive cracks in a heterogeneous material

Pierre-Philippe Cortet, Guillaume Huillard, Loïc Vanel and Sergio Ciliberto

Laboratoire de physique, CNRS UMR 5672, Ecole Normale Supérieure de Lyon,
Université de Lyon, 46 allée d'Italie, 69364 Lyon Cedex 07, France

E-mail: Loic.Vanel@ens-lyon.fr

Résumé. We study experimentally the paths of an assembly of cracks growing in interaction in a heterogeneous two-dimensional elastic brittle material submitted to uniaxial stress. For a given initial crack assembly geometry, we observe two types of crack path. The first one corresponds to a repulsion followed by an attraction on one end of the crack and a tip to tip attraction on the other end. The second one corresponds to a pure attraction. Only one of the crack path type is observed in a given sample. Thus, selection between the two types appears as a statistical collective process.

Keywords : Crack interactions, Crack paths, Pattern, Fracture mechanics, Heterogeneous materials

1. Introduction

Understanding the rupture mechanisms of solids has become an important goal of fracture physics in order to improve the strength of structures and avoid catastrophic failures. Characterization of rupture properties very often involve the growth of a dominant crack. For instance, there is an extensive literature, both experimental and theoretical, discussing the slow growth dynamics of a single crack along a straight path in brittle [1, 2, 3, 4, 5, 6, 7] or visco-plastic materials [8, 9, 10, 11, 12, 13, 14, 15]. However, in many practical situations, the crack path is not straight. For one thing, the crack path can be slightly destabilized and develop some roughness due to dynamical instabilities [16] or material heterogeneities. This kind of path instability has motivated a large amount of experimental works analyzing the roughness of cracks [17, 18, 19, 20, 21, 22, 23] as well as several models describing roughening mechanisms [24, 25, 26] and non-trivial effects of heterogeneities on the rate of crack growth [27, 28, 29]. Much larger deviations of the crack path from a straight line can be observed during the growth of an array of interacting cracks. Comparatively to the case of roughness, this rather complex situation has been studied essentially theoretically [30, 31, 32, 33, 34, 35, 36] and very little experimentally [37, 38, 39] despite its practical importance especially for heterogeneous materials where multiple cracks are likely to form. Understanding the growth of interacting cracks is also a relevant issue for fault dynamics [40] as well as crack pattern formation during drying processes [41, 42, 43, 44].

There are several levels of complexity that can play a role in the growth of interacting cracks. First, depending on the geometry of the crack array and the loading, the stress field around a crack will be amplified or shielded because of the existence of other cracks. Then, in $2d$, the effective contribution of the loading on each crack will usually be a mixture of mode I and mode II ‡. It has been argued that crack deviations occur when the shear stress on the crack lips (mode II) is non-zero and that the crack will grow so as to minimize the mode II contribution and maximize the mode I contribution [45, 46, 47]. A noticeable observation related to this property is the preferential merging of cracks joining each other forming a right angle, commonly observed for crack patterns in drying experiments [42, 43, 44]. This occurs naturally because the principal stress along a crack lip is parallel to the crack direction so that a crack approaching the lip with a right angle is propagating mainly in mode I. On the other hand, when two collinear mode I cracks are growing towards each other, they do not merge tip to tip, but instead repel each other [37]. The origin of this effect has been discussed by several authors [30, 32] and numerical simulations have been able to reproduce, at least qualitatively, experimental observations [34]. However, there are not many experimental data to compare with these theoretical predictions, and furthermore, there is very little knowledge about the effect of material heterogeneities on the crack path selection.

‡ The mode I corresponds to a tensile stress normal to the plane of the crack as the mode II corresponds to a shear stress acting parallel to the plane of the crack and perpendicular to the crack front.

In this paper, we study experimentally the trajectories of interacting cracks in an almost two dimensional brittle and heterogeneous material. The array of cracks has been initiated prior to the application of the external stress and the heterogeneity of the material (paper sheets) allows us to test the stability of crack paths to small perturbations. We uncover that for a given geometry of the crack array, a crack can follow statistically two stable trajectories : an attractive one and a repulsive one with respect to the neighboring cracks. The main result of this investigation is the analysis of the geometrical conditions for which cracks are attracted towards another and when they are repelled. The paper is organized as follows. In the next section, we describe the experimental apparatus. In section 3, the extraction procedure of the post-mortem shapes of the crack profiles is described. In sections 4, 5 and 6, we analyze the different types of crack paths and their statistics as a function of the initial crack pattern geometry. In section 7, we finally discuss the results and conclude.

2. The experiments

To study the growth of several interacting cracks, we have loaded bi-dimensional brittle samples made of fax paper sheets (Alrey[®]) with a tensile machine. The samples were previously prepared cutting several straight cracks in the paper sheets. In order to observe clearly the interaction between cracks during their growth, we had to find a geometry for which all crack tips are equivalent. Actually, we wanted to prevent the isolated growth at a particular crack tip that will inhibit the growth of the other cracks. One possible geometry that follows this condition consists in an array of cracks as presented in figure 1. The pattern formed by the two lines of cracks offers the advantage to have some translational invariance in the cracks direction. The stress is applied perpendicularly to the cracks direction and uniformly on the sample borders. Therefore, stress intensification is theoretically equivalent at each crack tip. In this geometry, there are three adjustable parameters : the crack length, the vertical spacing of cracks on a line and the horizontal spacing between the two lines. In this article, the first two parameters are fixed to 1cm and only the distance d between the two lines of cracks has been varied.

Each sample is prepared with the 11 initial cracks forming the array using a cutter blade. The experimental set-up consists of a tensile machine driven by a motor (Micro Controle UE42) controlled electronically to move step by step (Micro Controle ITL09). The paper sheets are mounted on the tensile machine with both ends attached with glue tape and rolled twice over rigid bars clamped on jaws. The motor controls the displacement of one jaw (400 steps per micrometer) while the other jaw is rigidly fixed to a force gage (Hydrotonics-TC). The tensile machine is placed in a box with a humidity level stabilized at 5% and at room temperature. The samples are loaded by increasing the distance between the jaws on which they are clamped such that the resulting force $F = \sigma eH$ ($e = 50\mu\text{m}$ is the film thickness and $H = 20.95\text{cm}$ the sample height) is perpendicular to the initial cracks direction. The loading is enforced at a constant and

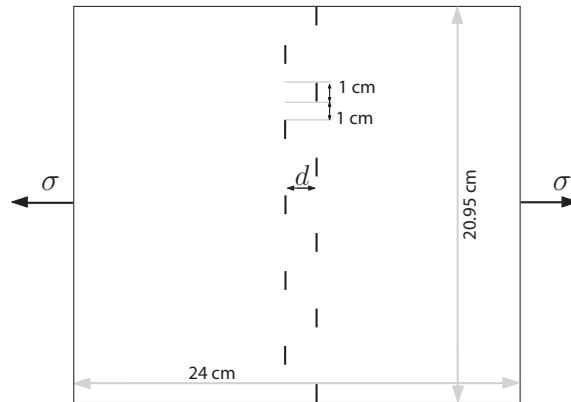


FIG. 1 – Geometry of the crack array initiated in the paper sample and the direction of the applied stress σ .

very slow velocity (between $0.84\mu\text{m}\cdot\text{s}^{-1}$ and $2\mu\text{m}\cdot\text{s}^{-1}$) until the final breakdown of the sample. More details about the experimental set-up can be found in [7]. Actually, once the force threshold F_c of the sample is overcome, we observe a quasi-instantaneous rupture of the sample with a quasi-simultaneous growth of all the cracks. There is no visual evidence of any sub-critical crack growth process before the final breakdown of the sample. During this breakdown, the applied force drops. When it reaches about half its maximum value, we stop loading the sample before breaking it in two pieces. It is a convenient procedure that allows us afterwards to image properly the crack path configurations in each sample.

3. Post-mortem analysis of crack trajectories

After each experiment, post-mortem samples are digitized using a high resolution scanner. The obtained images are processed in order to get a binary image in which the crack paths can be distinguished. In figure 2, we show an example of a digitized sample and of the corresponding extracted binary image. This image processing allows to finally create for each crack path the profile $y(x)$ that describes its shape as a function of the abscissae x along the axis corresponding to the initial crack direction and centered on the corresponding initial crack (cf. figure 3).

4. Two types of crack path

For an horizontal spacing $d = 0\text{cm}$ between the two crack lines, the initial crack array collapses into a single crack line. In figure 4, one can see that the crack paths show a repulsion phase before an attraction one. This initial crack pattern always leads to the so-called type B_0 growth behavior. This is the signature of the fact crack tips repulse each other. Indeed, the crack tips move away from the initial crack line before the neighboring tips overtake each other. Then, the paths curve to join the neighboring

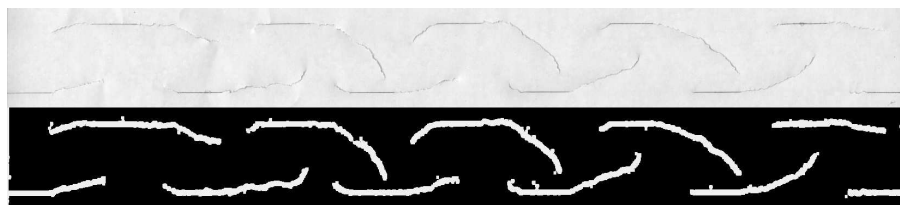


FIG. 2 – Post-mortem images of a fractured sample with $d = 1.5\text{cm}$: at the top, initial digitized image and, at the bottom, corresponding binary image with extracted crack paths obtained through image processing.

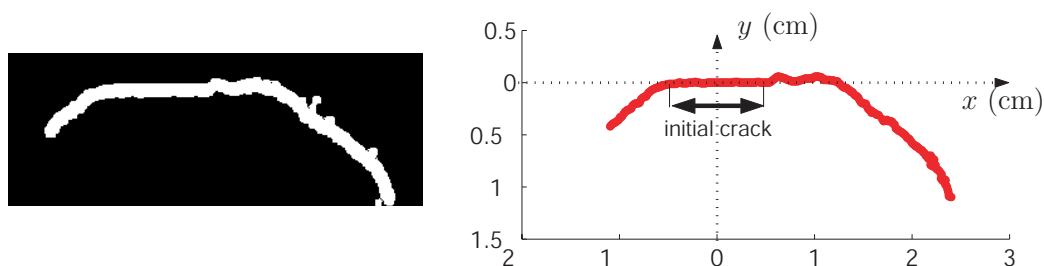


FIG. 3 – On the left, binary image showing the path followed by a crack, and on the right, corresponding extracted crack profile $y(x)$.



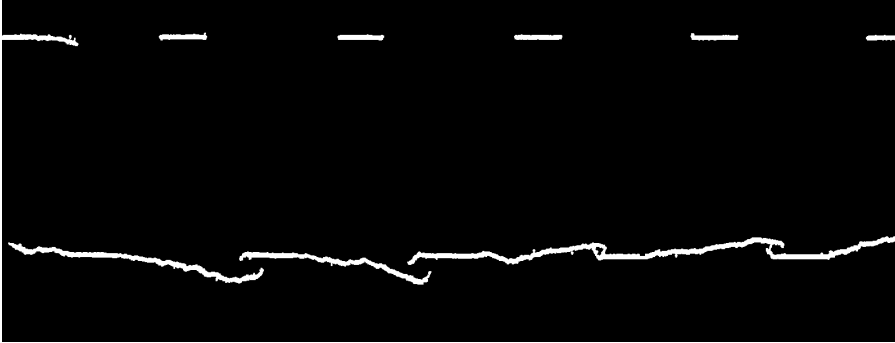
FIG. 4 – Binary image of a fractured sample with $d = 0\text{cm}$.

crack lips tending to form a right angle. Couples of crack paths appear to describe a sort of spiral shape as one can see in figure 5.



FIG. 5 – Close-up of a binary image of a fractured sample with $d = 0\text{cm}$.

For $0 < d < d_{\text{int}}$ (experimentally $d_{\text{int}} \approx 1.8 \pm 0.2\text{cm}$), two different kinds of behavior have been identified with respect to the crack path shapes among the fifty crack arrays that have been fractured. These two behaviors occur statistically for a given sample geometry. For the first one, that will be referred to as type A, neighboring cracks on different lines attract each other from the beginning of the crack growth up to the end as it is the case in figure 2 ($d = 1.5\text{cm}$). In contrast, for the type B, the crack paths are a mixture of two paths, a repulsive plus attractive path on one end and an attractive

FIG. 6 – Binary image of a fractured sample with $d = 0.4\text{cm}$.FIG. 7 – Binary image of a fractured sample with $d = 5\text{cm}$.

path tip to tip on the other end of each crack. For instance, in figure 6 ($d = 0.4\text{cm}$), we observe a repulsion phase for the right tip of the bottom cracks followed by an attraction phase by the neighboring crack on the other line while the right tip of the top cracks tends to join the left tip of the bottom cracks in a rather unexpected way. It seems that the symmetry breaking associated to the repulsive phase of crack growth on one end of the crack allows simultaneously the merging of tips on the other end of the crack.

Finally, when $d > d_{\text{int}}$, the two lines of cracks do not interact (cf. figure 7). Actually, one of the two lines fractures preferentially and we get the type B_0 behavior previously observed for $d = 0\text{cm}$ since the situation is comparable.

To summarize the results :

- For $d = 0$, only type B_0 is observed.
- For $0 < d < d_{\text{int}}$, types A and B are observed.
- For $d_{\text{int}} < d$, only type B_0 is observed.

The statistical proportion between types A and B is a function of the spacing d between the two initial crack lines. In figure 8, we plot for each value of d the percentage P of samples for which the fracture process follows type B (including the case B_0). This percentage decreases regularly starting from 100 % for $d = 0$ down to zero for $d = d_{\text{int}}$ where it jumps back brutally to 100% (this last case corresponds to rupture on a single crack line as observed in figure 7).

In the case of a homogeneous material, we would have expected the crack trajectories to be reproducible from one experiment to the other. A sheet of paper is actually made of a complex network of cellulose fibers. Scanning electron microscopy on our samples shows fiber diameters between 4 and $50\mu\text{m}$ with an average of $18\mu\text{m}$. Cellulose fibers are themselves a bundle of many microfibrils that have a crystalline structure [48]. The statistical selection between two types of crack path shapes for a

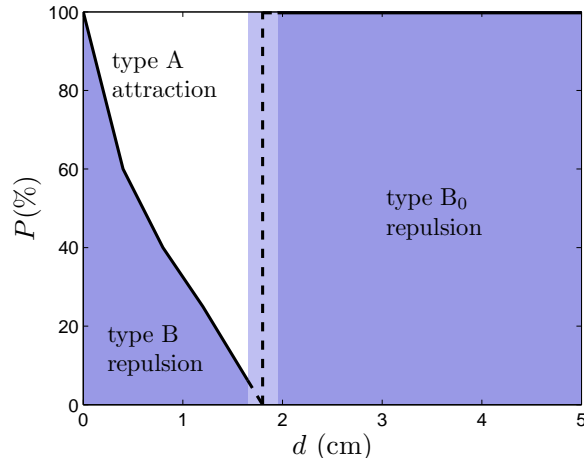


FIG. 8 – Percentage of samples for which the crack path are of type B (including the case B_0). Experimentally, there is some uncertainty concerning the distance at which there is no more interactions between the two crack lines. This is schematically shown by the dotted line and lighter color band around $d = 1.8\text{cm}$.

given initial crack geometry is probably triggered by this heterogeneity of the fractured material. Indeed, heterogeneity and anisotropy in the initial crack tip toughness and shape due to the heterogeneity of the material might induce small perturbations in the initiation of the crack growth path. We discover that these perturbations are large enough for the crack to explore statistically two very different “meta-stable” crack paths.

Additionally, the crack patterns observed in this section allow us to confirm the fact that, in general, two crack tips repulse each other while a crack tip and a crack lip attract each other.

5. Analysis of attractive cracks in type A samples

In this section, we study the average behavior followed by type A cracks that corresponds to experiments in which the cracks have been attracting each other during their whole growth. For each value of the spacing d between the two crack lines, we extract the average profile of the cracks. Actually, for each sample, we compute the mean crack profile $\langle y(x) \rangle$ averaging over the profiles $y(x)$ of all the cracks located on the same initial crack line. In figure 9(a), we plot for three different samples the averaged profiles of the two crack lines separated by $d = 1.2\text{cm}$. Then, we average the profiles $\langle y(x) \rangle$ over all the type A samples corresponding to the same value of d (cf. figure 9(b)). We get the mean type A profile $\langle\langle y(x) \rangle\rangle$ for each value of d .

It is important to notice that, depending on the position x , the number of profiles on which the averaging is performed is variable since all the cracks do not have the same length in the x direction. This is the reason why the averaged profiles, $\langle y(x) \rangle$ and $\langle\langle y(x) \rangle\rangle$, are not continuous at all points. For the same value of d , cracks of different

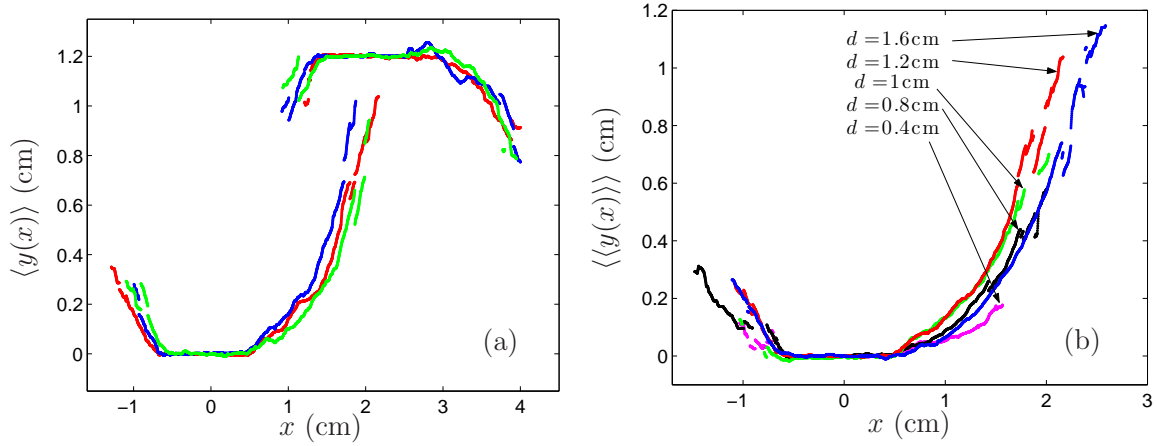


FIG. 9 – (a) Average crack profile $\langle y(x) \rangle$ for three samples with $d = 1.2$ cm and (b) average crack profile $\langle\langle y(x) \rangle\rangle$ for five values of d , for experiments with a type A behavior.

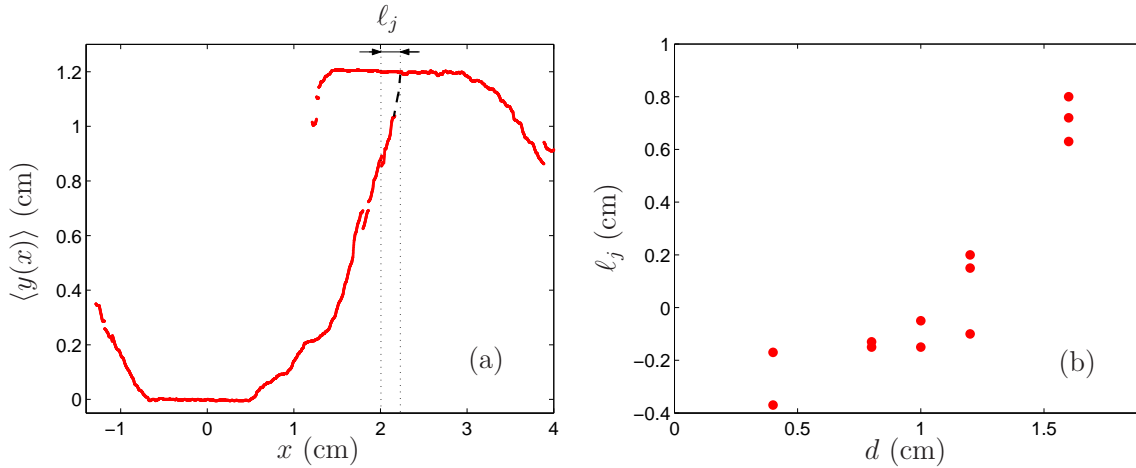


FIG. 10 – (a) Average crack profile $\langle y(x) \rangle$ for a sample with $d = 1.2$ cm and its extension allowing to define ℓ_j and (b) distance ℓ_j as a function of the spacing d between initial crack lines, for experiments with a type A behavior. Each point corresponds to one experiment.

samples appear to have very similar mean profiles $\langle y(x) \rangle$ as one can see in figure 9(a). Additionally, for all type A cracks, the dependence of the crack path on the distance between the initial crack lines d is weak and non-systematic. The main difference is that the crack paths extend farther away when the distance d is increased (cf. figure 9(b)).

Extending intuitively each crack path to join the neighboring crack lip on the other crack line, we are able to define an hypothetical junction position ℓ_j measured from the center of the joined crack (cf. figure 10(a)). In figure 10(b), we see that this junction distance ℓ_j increases rapidly with d . Actually, the rapid increase of this distance between $d = 1.2$ cm and $d = 1.6$ cm suggests that there might be a divergence of the junction position ℓ_j when the distance d approaches $d_{\text{int}} (\approx 1.8$ cm). A divergence of ℓ_j would

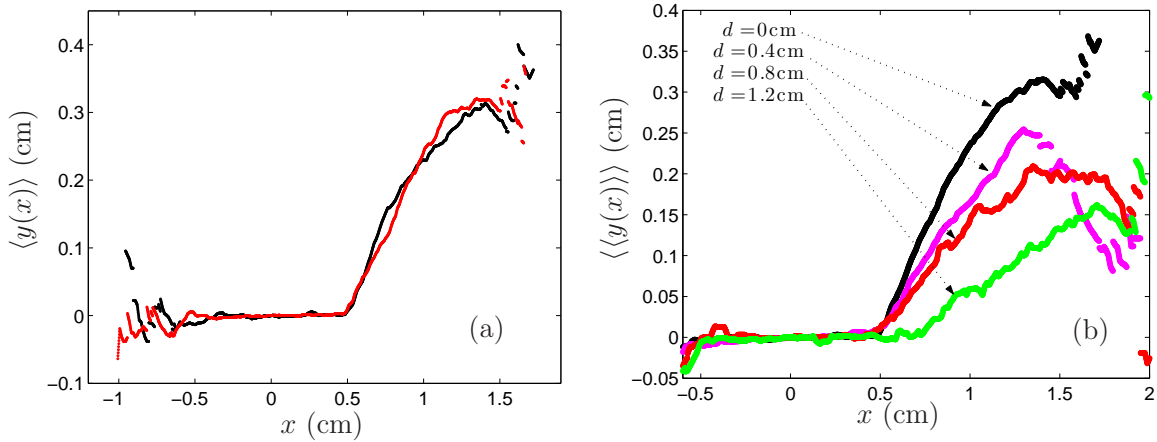


FIG. 11 – Paths of repelled cracks (type B). (a) Average crack profile $\langle y(x) \rangle$ for two samples with $d = 1\text{cm}$, and (b) average crack profile $\langle\langle y(x) \rangle\rangle$ for four value of d .

make sense since when $d > d_{\text{int}}$ the two crack lines do not interact anymore and thus, the cracks of one line cannot cross those of the other line.

6. Analysis of repulsive cracks in type B samples

In this section, we study in type B (including B_0 for $d = 0$) samples the average behavior followed by the repulsive crack paths. In figure 11(a), we plot the average profile of repulsive cracks $\langle y(x) \rangle$ for two samples with $d = 1\text{cm}$. We note that, for a given distance d , the crack path is reproducible from one sample to the other. In figure 11(b), we plot the average crack profile $\langle\langle y(x) \rangle\rangle$ as a function of d and x . Clearly, the smaller d , the larger the repulsion. One way to quantify this is to measure the maximum angle of deviation θ_{max} during the repulsion phase. As can be seen in figure 12, this quantity decreases with the distance d . If we extend linearly this curve, we can see that the effects of the repulsion disappear when d reaches a value of about 1.9cm . Interestingly, we recover a value in the range corresponding to the characteristic distance d_{int} above which the two crack lines do not interact.

For $d = 0$, we find a maximum deviation angle $\theta_{\text{max}} \simeq 27^\circ$. This value is significantly larger than Kachanov's prediction $\theta_{\text{max}} \simeq 14^\circ$ [32] that was obtained assuming the crack goes in the direction for which the strain energy release rate would be maximum. Melin [30] has a different approach to explain the deviation of collinear cracks. She analyzes the stability of the crack path to a local perturbation. The crack deviation angle is then $\theta = \text{atan}(2\delta y/L)$ where δy is the amplitude of the local deviation and L is the crack length. To obtain $\theta_{\text{max}} \simeq 27^\circ$ would require a perturbation $\delta y \simeq L/4 = 0.25\text{cm}$, a rather unphysical value. A large deviation angle could also be obtained assuming that several smaller local deviations of the crack path occur due to the heterogeneous structure of paper. However, if that was the case, one would expect the crack to progressively rotate instead of turning rather abruptly (see figure 11(b)).

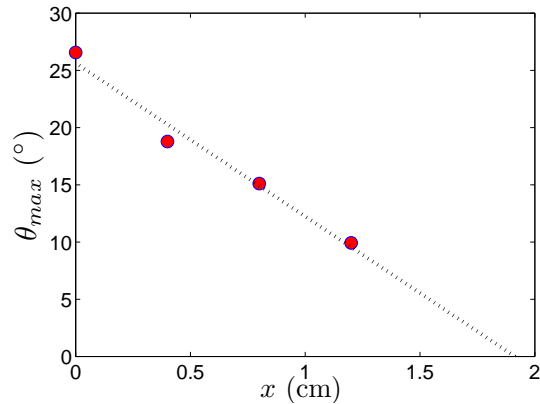


FIG. 12 – Maximum angle of repulsion of the crack path during the repulsion phase as a function of the distance d for type B experiments.

7. Discussion and conclusion

In this article, we have seen that the interactions between two lines of cracks growing under a very low strain rate in a heterogeneous material lead to a statistical behavior. Indeed, for the same initial sample geometry, we get two types of crack path pattern. The type A behavior, that corresponds to a permanent attraction between the cracks during their growth, appears to present a universal shape that does not depend significantly on the initial crack array geometry. On the contrary, for type B behavior, for which the crack paths present either a repulsion phase followed by an attraction or an attraction phase tip to tip, the path trajectories appear to be dependent on the distance between the two initial crack lines d . Indeed, the repulsion decreases as d increases and finally totally disappears as d tends to a certain distance d_{int} . This particular value of d is also a critical value above which the two lines do not interact anymore. Understanding this value is still an open issue. Also, the value of the crack deviation angle observed in our experiments during the repulsive phase remains unexplained. In particular, it is rather large compared to theoretical predictions.

The statistics observed for the crack path shape is the signature of the meta-stability of two types of crack trajectory for a given geometry. This bi-stability is for the moment an unexplained property but it seems to be intrinsic to the chosen crack pattern geometry. It is likely that the trigger for this statistics comes from the complex structure of paper sheets that makes this material heterogeneous and leads to anisotropy on the initial crack tip shape and toughness. The two types of crack path are two meta-stable paths between which each crack has to choose when it initiates its growth. Only at this initiation stage, may the heterogeneity of the sample strongly influence the crack in its “choice”.

It is also important to point out the collective behavior of the cracks located on the same initial crack line. Indeed, inside a given crack line, all the cracks select a specific dynamics with quasi-identical crack path shape. Actually, the initiation of the global

rupture of a sample is probably triggered at one particular crack tip. The choice for the crack shape type is made at this particular moment. Then, an unexplained collective effect operates to make all the cracks throughout a line behave the same way.

Acknowledgments

This work was funded with grant ANR-05-JCJC-0121-01.

References

- [1] Hsieh C and Thomson R, 1973 *J. Appl. Phys.* **44** 2051
- [2] Rice J R, 1979 *Proceedings of the 8th U. S. National Congress of Applied Mechanics* (Western Periodicals, North Hollywood) p 191
- [3] Marder M, 1996 *Phys. Rev. E* **54** 3442
- [4] Santucci S, Vanel L, Scorretti R, Guarino A and Ciliberto S, 2003 *Europhys. Lett.* **62** 320
- [5] Santucci S, Vanel L and Ciliberto S, 2004 *Phys. Rev. Lett.* **93** 095505
- [6] Santucci S, Cortet P-P, Deschanel S, Vanel L and Ciliberto S, 2006 *Europhys. Lett.* **74**(4) 595
- [7] Santucci S, Vanel L and Ciliberto S, 2007 *Eur. Phys. J. Special Topics* **146** 341
- [8] Schapery R A, 1975 *Int. J. Fracture* **11** 141
- [9] Schapery R A, 1975 *Int. J. Fracture* **11** 369
- [10] Schapery R A, 1975 *Int. J. Fracture* **11** 549
- [11] Kaminskii A A, 1979 *Soviet. Appl. Mech.* **15** 1078
- [12] Kaminskii A A, 2004 *Int. Appl. Mech.* **40** 829
- [13] Chudnovsky A and Shulkin Y, 1999 *Int. J. Fracture* **97** 83
- [14] Cortet P-P, Santucci S, Vanel L and Ciliberto S, 2005 *Europhys. Lett.* **71**(2) 1
- [15] Cortet P-P, Vanel L and Ciliberto S, 2007 *Phys. Rev. Lett.* **99** 255502
- [16] Boudet J-F and Ciliberto S, 2000 *Physica D* **142** 317
- [17] Schmittbuhl J and Måløy K J, 1997 *Phys. Rev. Lett.* **78** 3888
- [18] Boffa J, Allain C and Hulin J-P, 2000 *Physica A* **278** 65
- [19] Salminen L I, Alava M J and Niskanen K J, 2003 *Eur. Phys. J. B* **32** 369
- [20] Mallick N, Cortet P-P, Santucci S, Roux S G and Vanel L, 2006 *Phys. Rev. Lett.* **98** 255502
- [21] Santucci S, Mathiesen J, Måløy K J, Hansen A, Schmittbuhl J, Vanel L, Delaplace A, Bakke J O H and Ray P, 2007 *Phys. Rev. E* **75** 016104
- [22] Célarié F, Prades S, Bonamy D, Ferrero L, Bouchaud E, Guillot C and Marlière F, 2003 *Phys. Rev. Lett.* **90** 075504
- [23] Bonamy D, Ponson L, Prades S, Bouchaud E and Guillot C, 2006 *Phys. Rev. Lett.* **97** 135504
- [24] Ramanathan S, Ertas D and Fisher D S, 1997 *Phys. Rev. Lett.* **79** 873
- [25] Schmittbuhl J, Roux S, Vilotte J-P and Måløy K J, 1995 *Phys. Rev. Lett.* **74** 1787
- [26] Bonamy D, Santucci S and Ponson L, *Preprint arXiv :0803.0190*
- [27] Kierfeld J and Vinokur V M, 2006 *Phys. Rev. Lett.* **96** 175502
- [28] Cortet P-P, Vanel L and Ciliberto S, 2006 *Europhys. Lett.* **74**(4) 602

- [29] Guarino A, Vanel L, Scorretti R and Ciliberto S, 2006 *J. Stat. Mech.* P06020
- [30] Melin S, 1983 *Int. J. Fracture* **23** 37
- [31] Hori M and Nemat-Nasser S, 1987 *J. Mech. Phys. Solids* **35** 601
- [32] Kachanov M, 1994 *Adv. Appl. Mech.* vol 30 (Academic Press, San Diego) p 259
- [33] Kachanov M, 2003 *Int. J. Fracture* **120** 537
- [34] Seelig T and Gross D, 1999 *J. Mech. Phys. Solids* **47** 935
- [35] Xia Z C and Hutchinson J W, 2000 *J. Mech. Phys. Solids* **48** 1107
- [36] Brener E A, Müller-Krumbhaar H and Spatschek R, 2001 *Phys. Rev. Lett.* **86** 1291
- [37] Eremenko A S, Novikov S A and Pogorelov A P, 1979 *J. Appl. Mech. Tech. Phys.* **20**(4) 477
- [38] Dolotova N A, Aleshin V I, Zeiliger V A and Bessonov M I, 1987 *Strength Mater.* **19** 886
- [39] Broberg K B, 1987 *Eng. Fract. Mech.* **28** 663
- [40] An L-J, 1998 *Tectonophysics* **293** 45
- [41] Groisman A and Kaplan E, 1994 *Europhys. Lett.* **25** 415
- [42] Shorlin K, de Bruyn J, Graham M and Morris S, 2000 *Phys. Rev. E* **61** 6950
- [43] Bohn S, Pauchard L and Couder Y, 2005 *Phys. Rev. E* **71**(4) 046214
- [44] Bohn S, Platkiewicz J, Andreotti B, Adda-Bedia M and Couder Y, 2005 *Phys. Rev. E* **71**(4) 046215
- [45] Erdogan R and Sih G C, 1963 *J. Basic Eng.* **85** 519
- [46] Goldstein R V and Salganik R L, 1974 *Int. J. Fracture* **10** 507
- [47] Cotterell B and Rice J R, 1980 *Int. J. Fracture* **16** 155
- [48] Jakob H F, Tschegg S E and Fratzl P, 1994 *Struct. Biol.* **133** 13