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RESEARCH ARTICLE

Single Shot Generation of High-Aspect-Ratio Nano-Rods from Sapphire by Ultrafast First Order Bessel Beam

Valeria Viviana Belloni,* Mostafa Hassan, Luca Furfaro, Remo Giust, Anne-Magali Seydoux-Guillaume, Sergio Sao-Joao, and Francois Courvoisier*

Engineering the polarization and spatial phase of ultrafast laser pulses represents a compelling strategy for enhancing control over laser–matter interaction and enabling rapid and innovative nano-fabrication processes. Here, the single-shot, ultrafast laser fabrication of high-aspect-ratio, vertically standing nano-pillars with a diameter of ≈ 800 nm and height up to $15\ \mu\text{m}$ on the surface of sapphire, is reported. To achieve this, the distinctive properties of diffraction-free, first-order Bessel beams endowed with either radial or azimuthal polarization distributions, are harnessed under tight focusing conditions. The highly intense laser–matter interaction in this configuration generates a tubular-shaped, high-pressure field beneath the material surface, leading to the rapid expulsion of material across the surface. Three distinct regimes for the pillar generation are identified in addition to a mechanism based on the Rayleigh-Plateau theory that explains the distinct morphological regimes observed. The findings not only shed light on the underlying physical mechanisms of intense excitation of transparent dielectrics but also offer exciting prospects for the rapid fabrication of positive nano-structures and material compression across various fields of application.

processing, enabling precise manipulation of matter.^[1–5] Specifically, radial polarization has emerged as a particularly appealing approach for laser drilling since it favors the phenomenon of resonance absorption, which enhances the efficient transfer of energy from the laser to the material surface.^[6,7] The ability to control polarization patterns across the beam empowers a wide variety of sophisticated textures both on the surface and within the bulk of materials.^[8,9] For instance, by exerting control over the local polarization orientation, complex orientation patterns of laser-induced periodic surface structures can be precisely tailored, while the plasmonic field enhancement induced by polarization plays a significant role in determining the depth of these structures.^[10,11] Additionally, beams featuring polarization states that evolve during propagation have enabled the fabrication of chiral structures within the bulk of fused silica.^[12]

1. Introduction

Integration of innovative beam, polarization, and temporal shaping has yielded remarkable progress in the field of material

Optical vortices have also emerged as effective tools for manipulating laser–matter interaction. In Gaussian laser beams, the phase singularity is responsible for doughnut-shaped cross-sections. Interestingly, the vortex carried by the optical pulse can be transferred to the material, resulting in the generation of nano-needles with helical surface sub-structures on tantalum,^[13,14] silicon,^[15] silver,^[16] and aluminum^[17] through single-shot ablation. Vortex beams have also been employed to create other intricate structures such as nano-domes,^[18] 3D chiral structures,^[19] and spiraling fibers.^[20]

Bessel beams offer a fascinating class of solutions to the Helmholtz equation due to their inherent propagation invariance.^[21,22] Unlike Gaussian beams, Bessel beams exhibit an extended focal region that surpasses the equivalent Rayleigh range by several orders of magnitude. A zeroth-order Bessel beam is a cylindrically-symmetric interference field that can be produced using an axicon^[23] or a spatial light modulator.^[24] For sufficiently high focusing angles, the nonlinear propagation of ultrashort pulses inside transparent dielectrics is highly stable with negligible influence from the nonlinear Kerr effect.^[25] This regime allows for energy deposition of a single ultrashort pulse along a high-aspect ratio nano-plasma, which evolves within tens of microseconds,^[26] into a high-aspect ratio nano-void inside glasses or sapphire, with important applications for

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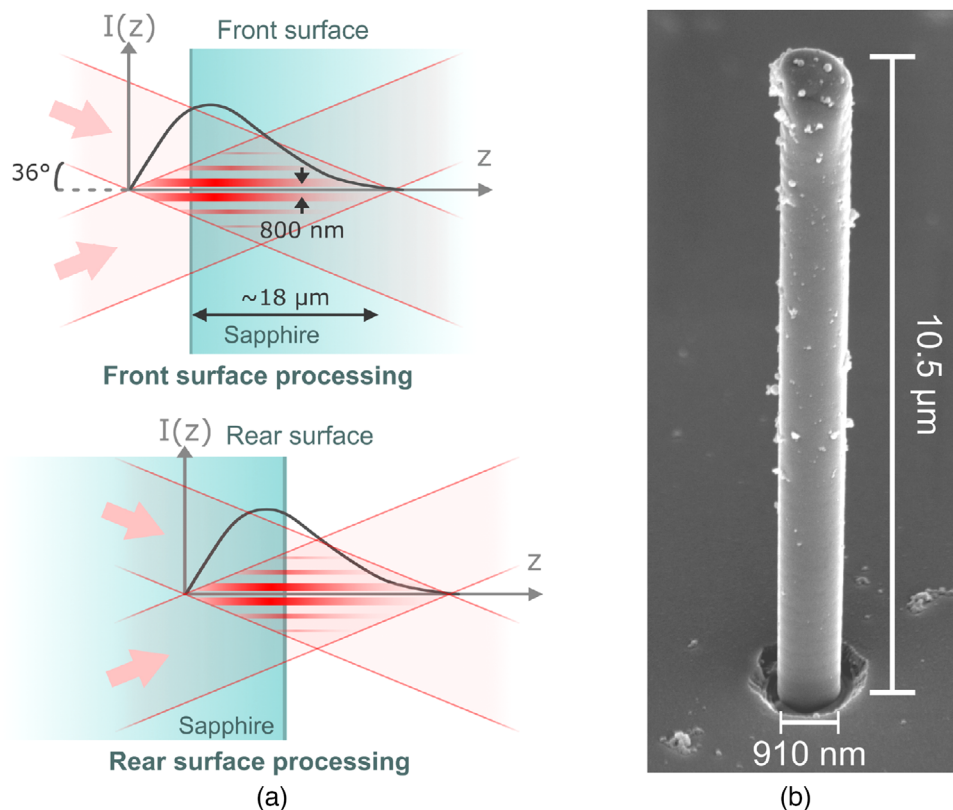


Figure 1. a) Concept of the laser illumination strategy. A first-order, ultrafast Bessel beam is focused across the sample front or exit surface. The focal region is shaped as a hollow cylinder surrounded by several rings. The solid black line sketches the intensity of the cylinder along the propagation. In each configuration, the intensity is kept higher inside the bulk than on the surface. b) Example of a nano-pillar produced after single shot illumination on the sample back surface, in radial polarization, 115 fs pulse duration.

high-speed cutting ($\approx 1\text{ m s}^{-1}$) or for the nano-fabrication of sensors.^[27–33]

Importantly, higher-order Bessel beams, which carry a vortex charge, possess a focal region in the shape of a high-aspect-ratio hollow cylinder. Their stability in the nonlinear, ultrashort pulse regime has been demonstrated.^[34] The violent material phase change produced in the wake of the single shot laser illumination inside transparent dielectrics,^[35] emitting shockwaves,^[36] lets us expect that a cylindrical beam shape allows for compressing materials inside the cylinder. A proof-of-principle has already been obtained in glass by Xie et al., with a single pulse shaped as a higher-order Bessel beam with circular polarization to generate a high-refractive index rod inside the bulk of glass.^[37]

Recent results have shown that zeroth-order Bessel beams induce, in a single shot, a very high energy density plasma,^[38] thanks to the process of resonance absorption,^[39] which occurs for polarization oriented perpendicular to the nano-plasma rod. With the aim of generating extreme states of matter, we have used a radially-polarized first-order Bessel beam, with a focal region shaped as a high-aspect ratio cylinder with an 800 nm diameter. Here, we report, for the first time to our knowledge, the generation of high aspect ratio nano-pillars vertically standing on the surface of sapphire. The positive structure is created by the high pressures generated below the material surface by ultrashort first-order Bessel pulse. Straight rods and wavy types of

nano-pillars have been generated, with lengths up to $15\text{ }\mu\text{m}$. We have identified a model to explain the three different regimes observed, that range from the extrusion of quasi-solid material to the jet of liquid material, where capillary instabilities are observable. We also investigate the role of pulse duration and polarization in the nano-pillar formation process.

2. Nano-Pillars Generation from the Sapphire Surface

Figure 1a shows a concept of our experiments. We studied the interaction of a radially or azimuthally polarized first-order Bessel beam crossing the front or the exit surface of a sapphire sample. The beam is produced from a primary femtosecond, linearly polarized zeroth-order Bessel beam^[24] using a spatially variant half-waveplate. The beam cross-section features a doughnut-shaped focus, surrounded by several rings of lower intensity. The Bessel beam is characterized by a cone angle of 36° (equiv. numerical aperture 0.6), which imposes a doughnut diameter of $\approx 800\text{ nm}$, which extends over a propagation length of $\approx 20\text{ }\mu\text{m}$ (FWHM) in air, that is, $35\text{ }\mu\text{m}$ in sapphire. Technical details are provided in Experimental Section, and the experimental beam characterization is shown in Figure S1, Supporting Information.

We first investigate focusing of the Bessel beam across the sample exit side, using 115 fs pulses, with energies ranging from 4.4 to $7\text{ }\mu\text{J}$ at the sample site. A representative outcome of the

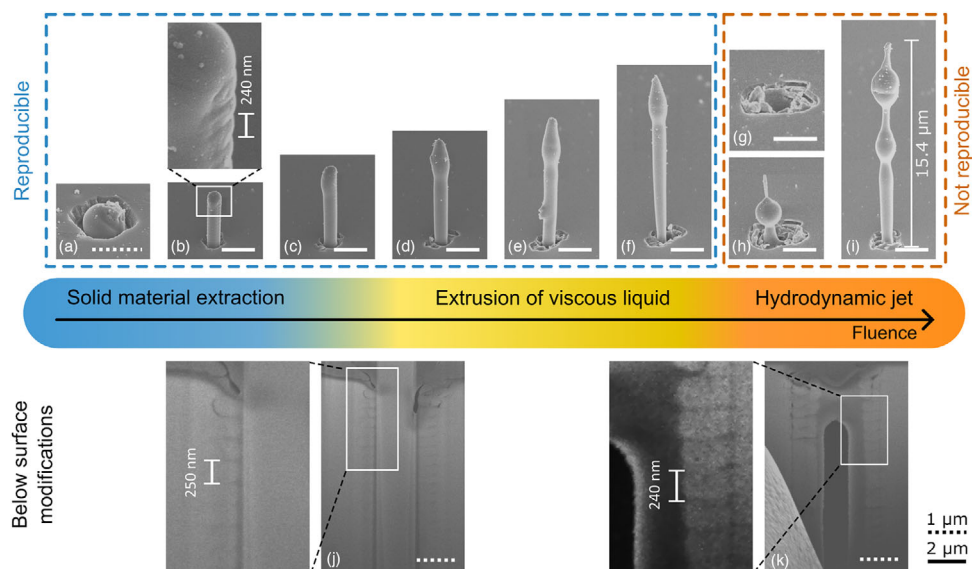


Figure 2. Evolution of the nano-pillar morphology depending on the main Bessel ring fluence. We used pulses with pulse duration of 115 fs, energy of 6.1 μJ , and different relative positions beam-sample. We can identify three different regimes depending on the beam fluence. In the case of the first and second regimes, the nano-pillars are reproducible (refer to Experimental Section for the reproducibility), while for higher fluence, the nano-pillars are no more reproducible from shot to shot. At the bottom of the figure, we show the modifications produced below the surface (see Experimental Section for more details). We also insert some close-ups to show smaller details. Scale bars are 2 μm for the solid ones and 1 μm for the dashed ones.

intense laser-matter interaction is depicted in Figure 1b, demonstrating the generation of a high aspect ratio cylindrical nano-pillar from the surface. It has a diameter of ≈ 900 nm for a height exceeding 10 μm . The primary objective of this paper is to elucidate the underlying mechanism responsible for the formation of this remarkable structure.

For each pulse energy, we have scanned the relative position of the surface within the beam by steps of 1 μm . The fluence of the main Bessel ring, that is, the fluence on the tubular focus, varies smoothly along the propagation. It is shown as a solid line in Figure 1a. Therefore, the fluence distribution in the material bulk varies at each step.

Figure 2 shows a series of scanning electron microscopy (SEM) images of the nano-structures produced after single-shot irradiation, for a pulse energy of 6.1 μJ at different positions in the beam, without further processing other than sample metallization for SEM imaging (see Experimental Section). We have characterized three different morphologies of high-aspect-ratio nano-pillars formed at the surface of the sapphire sample, which were ranked by the fluence at the sample surface. For the lowest fluences, we observe straight nano-pillars. In Figure 2b, the diameter of the nano-pillar is 800 nm for a height of 4.4 μm . Its surface shows a slight periodic corrugation, on which we will comment in the next section. At higher fluence, the second regime is featured by a slick surface and often small perturbations of the nano-pillar shape at the top of the structure. In this regime, we found a maximal pillar height of 13 μm with a typical diameter of 700 nm, leading to an aspect ratio of 21. The first two regimes are highly reproducible from shot to shot. At the highest surface fluences, the third regime presents nano-pillars with highly wavy structures. This regime is nearly stochastic. Figure 2g–i shows three different structures obtained in close conditions. Above this regime, only nano-droplets can be found at the sample's surface,

tens of micrometers away from the small crater, similarly as in Figure 2g.

3. Formation Mechanism of the Nano-Pillars

Here, we propose a model explaining the different nano-pillar formation regimes. We expect that the pulse propagation remains quasi-linear because of the high cone angle used. Therefore, the main ring of the radially-polarized Bessel beam generates a plasma distribution shaped like a high aspect ratio nano-tube (see **Figure 3**).^[34] The pressure and temperature on the tube increase sharply, potentially up to the warm dense matter regime.^[38,41] This leads to radial forces toward the tube center and outward, as in the case of surface excitation by an optical vortex.^[42] In our case, a long column of material is pressurized, and the relaxation involves material transfer from bulk across the surface. We notice that, in our conditions, the beam fluence is higher in the sapphire bulk than on the surface. It is probable that material is ejected because the pressure deep in the material bulk is higher than close to the surface. Similar high-pressure conditions were observed for zero-order Bessel beam, leading to the generation of nano-spheroid on YAG^[43] and in nano-channel formation with the so-called surface assisted material ejection.^[44]

Depending on the laser-deposited energy, the material at the center of the tube core can be in different physical states. As highlighted before, the three regimes we have identified depend on the fluence at the exit surface. This is obviously related to the energy deposition in the material close to the surface. Supposing that a higher fluence leads to a higher temperature in the material and to a material with lower viscosity and surface tension, we can understand the first regime as the translation of solid material, the second as the extrusion of high-viscosity fluid, and the

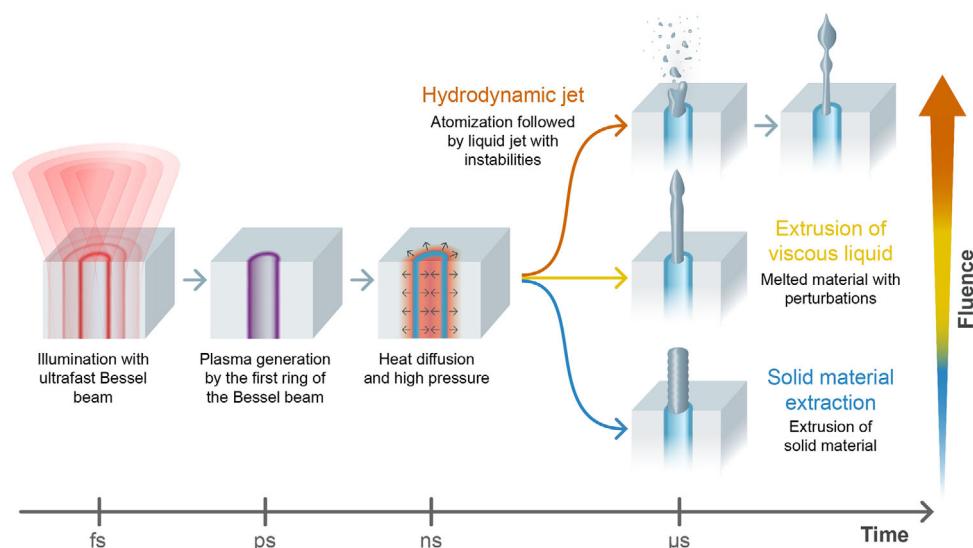


Figure 3. Concept of the nano-pillar formation mechanism for the three different regimes that can be controlled via the fluence. The process is identical if the laser pulse propagates from top to bottom or vice-versa. The timescales are estimated orders of magnitude from the literature.^[26,40]

third regime as the emission of low-viscosity liquid jet undergoing capillary instabilities. A concept figure with the stages of the nano-pillar generation is shown in Figure 3, and we comment on each regime in more detail in the paragraphs below.

3.1. First Regime: Translation of Rod-Shaped Solid Material

The first regime presents very regular nano-pillars and almost negligible effects of the beam around the nano-pillar base (in Figure 2a–c note the limited damage on the surface). We suppose that the main ring of the Bessel beam creates a thin cylindrical layer of liquid material while the internal rod of material remains solid due to the low fluence. The layer of liquid material and the high internal pressure allow the translation of the rod outside the bulk. It is possible that higher fluence, deeper into the bulk, creates higher pressure conditions, leading to the propulsion of a solid nano-rod out of the sapphire bulk. This first regime appears for fluences between 0 and 2 (a.u.) (All arbitrary unit fluences across the different figures are expressed using the same reference).

The translation mechanism is confirmed twofold. First, we remark on the presence of periodic nanostructures on the surface of the nano-pillars (see the horizontal lines in the close-ups of Figure 2b,j,k). They match very well the pattern observed in the material bulk, observed after focused ion beam (FIB) milling below the nano-pillars (bottom row in Figure 2). This clearly indicates that the material remains solid during the transformation and maintains the structures created beforehand. We note that the period of the horizontal nanostructures remains constant among the different parameters for which they are observed. These structures are attributed to highly localized material amorphization by an interference pattern between the onset of the Bessel pulse reflected on the exit surface and the trailing part of the Bessel beam. A simulation of the resulting intensity distribu-

tion is shown in Figure S2, Supporting Information. This interference has a period of $\frac{\lambda}{2n \cos \theta} = 241 \text{ nm}$, where λ is the central wavelength, n is the sapphire refractive index, and θ the Bessel beam cone angle in the medium, which is in excellent agreement with the experimental value of $\approx 240 \text{ nm}$. In this framework, the periodic pattern is inscribed before material ejection.

Second, we performed transmission electron microscopy (TEM) in bright field mode (BF) in addition to FIB investigations. The BF-TEM observations of the nano-pillar in Figure 2b is shown in Figure 4. The BF-TEM image (a) of a thin foil of the pillar and part of the bulk material show Bragg diffraction contrasts (dark lines) proving that both pillar and bulk sapphire are crystalline. Moreover, the close-up (b) and the associated selected area electron diffraction (SAED) pattern (c) performed in one zone axis ([3-2-2]) confirm that the pillar is a mono-crystal (c), as the initial sample material. In (a), the dark lines around the pillar, below the surface (see dashed ellipse), are characteristic of highly stressed material. They become denser when getting closer to the position of the cylindrical focus, that is, around the translated nano-rod. The periodic gray triangles (solid arrows), with a typical size of 50 nm observable below the surface around the nano-rod, are amorphous zones. Amorphization has been induced by the different phase transitions and fast cooling. The fact that the pillar is effectively a mono-crystal shows that it has not undergone any phase transition. In fact, the fast cooling of a liquid would result in a polycrystalline material, and not a well-formed monocrystal. Therefore, the nano-pillar generation is due to a translation of the rod from the material's bulk.

The nanopillar height varies both with the pulse energy and position of the beam inside the sample. As we will detail in Section 4, we have observed that the fluence reached on the sample surface is the most discriminatory parameter. We show in Figure 5 the evolution of the height of the nano-pillars as a function of the fluence on the sample surface. In the first regime, the nano-pillar height varies linearly with the fluence. The maximum

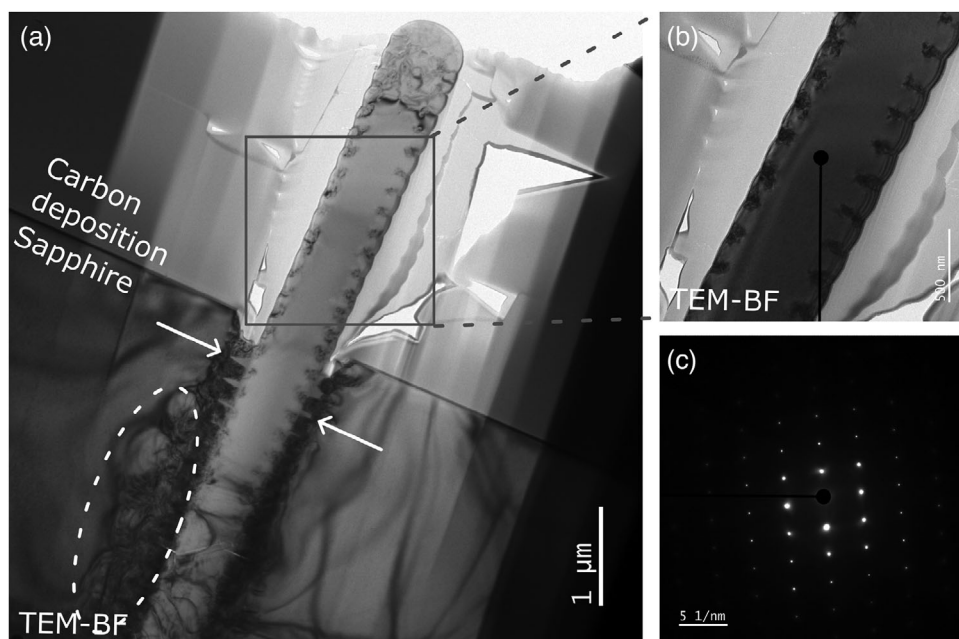


Figure 4. Transmission electron microscope (TEM) images of the nano-pillar shown in Figure 2b. a) Bright field TEM (BF-TEM) image shows a thin foil with the complete pillar and part of the bulk. The material on both sides of the pillar is a protection layer of carbon; its deposition is necessary for the FIB preparation. b) The close-up of the pillar and c) its selected area electron diffraction (SAED) pattern observed along [3-2-2] zone axis highlight the crystalline state of the pillar.

height reached in the first regime is also linked to the Bessel beam length inside the medium, which is typically $18\ \mu\text{m}$ (the effective insertion is shown in detail in Figure S3–S5, Supporting Information). We note that in this regime, as in the second, we did not observe a void below the nano-pillars. Either the material density has been highly depressed over a significant volume (note that sapphire density varies by $\approx 25\%$ between the solid and the molten states^[45]), or a void is present but below the maximal depth reached by FIB milling, that is, $\approx 10\ \mu\text{m}$.

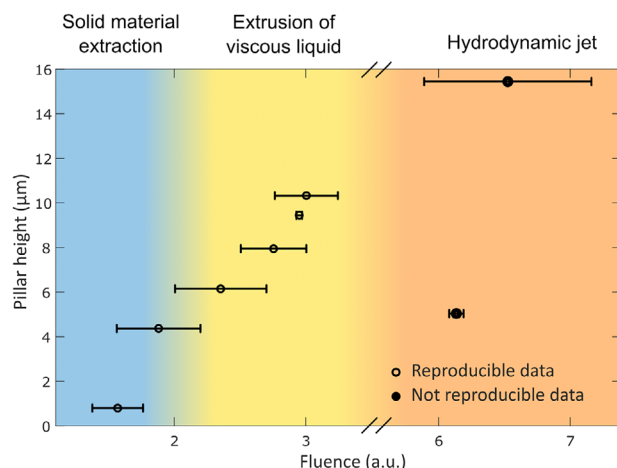


Figure 5. Height of the nano-pillars as a function of the main Bessel ring fluence on the exit surface for pulses with pulse duration of 115 fs, energy of $6.1\ \mu\text{J}$. The fluence is determined by the relative beam-sample position. The data corresponds to the nano-pillars shown in Figure 2.

3.2. Second Regime: Reproducible Nano-Pillars with Slick Surface

The nano-pillars of the second regime (Figure 2c–f), for fluences in the range of typically 2 to 3.5 a.u., present a slick surface: they do not show transverse periodic patterns. Most of the structures also present small perturbations at their extremities. We understand this regime as the extrusion of highly viscous liquid sapphire through the nozzle formed by the surface crater upon laser impact. We can notice that the structures produced in this regime have a smaller and smaller diameter from top to bottom: this can be explained by the progressive closing of the surface aperture because of simultaneous cooling during the extrusion. The small perturbations at the extremities can be due to the reshaping of the extruded rod because of internal stresses produced by temperature inhomogeneities. In this regime, since the surface of the pillar is molten, the periodic pattern vanishes.

We see in Figure 5, that in this regime, the nano-pillar height increases approximately linearly with the surface fluence as in the case of the first regime. It reaches a maximal value of $\approx 13\ \mu\text{m}$ in the second. (Note that the error bars along the fluence axis are large because the fluence profile of the Bessel beam is steep in some regions. For this reason, the $\pm 1\ \mu\text{m}$ error on the sample-beam position can transfer to large error bars on the fluence).

3.3. Jets with Capillary Instabilities

Before detailing the third regime, we briefly recall literature results on capillary instabilities as they are characteristic of this regime. Capillary instabilities are due to the fact that the surface energy of a cylindrical jet is not the minimum. Therefore,

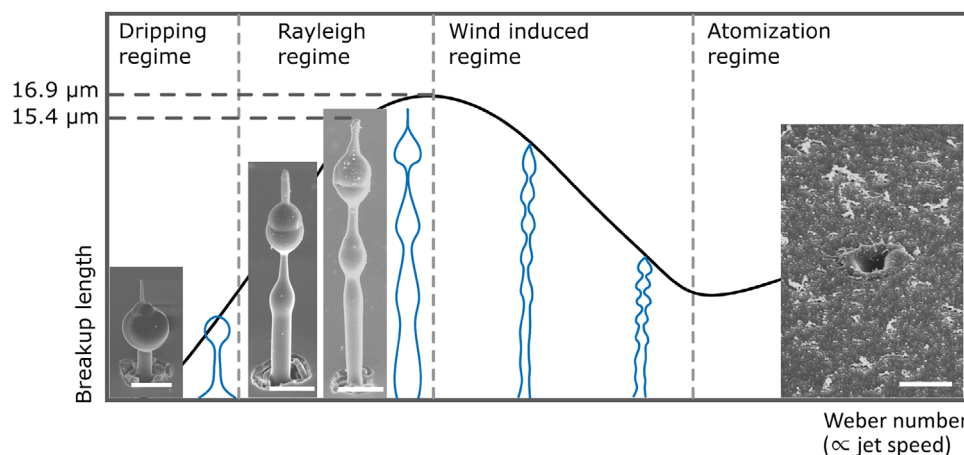


Figure 6. Evolution of the breakup length versus the jet speed or the Weber number (We) from the capillary instability theory, highlighting the different regimes.^[46] The blue shapes are profiles of real water jets in the three regimes (not in scale).^[50,51] The SEM images show examples of nano-pillars produced in the third regime, highlighting the high degree of correspondence between the two cases. Scale bars: 2 μm .

any perturbation tends to break the jet into segments or droplets as observed early by Plateau and Rayleigh.^[46] Capillary perturbations on jets of molten material were observed in previous laser-based processes, as in laser-induced nano-jetting from metallic films^[47,48] and in vortex beam machining of silicon.^[49] The theory that describes the behavior of liquid jets has been initially developed by Rayleigh and Plateau and was further completed as capillary instability theory.^[50] It distinguishes different regimes depending on the Weber number or the jet speed (see **Figure 6**). The Weber number is defined as $We = \rho v^2 d / \sigma$, where ρ is the density of the fluid, v is the jet speed, d is the jet diameter, and σ is the surface tension of the liquid.

In **Figure 6**, we show with solid blue lines the typical morphology of water jets for different jet speeds and Weber numbers from refs. [50, 51]. At low Weber numbers, the jets are cylindrically symmetric (dripping and Rayleigh regimes). Increasing the Weber number, the jet starts to be asymmetric (wind regime) and eventually reaches the atomization regime, where the jet sprays into particles much smaller than the nozzle diameter. (Dripping and Rayleigh regimes can easily be observed, for instance, in the coffee jet of an espresso machine.) In the same figure, the black solid line shows the evolution of the breakup length, for which the jet breaks into separate droplets.^[46]

The Weber number shows that the temperature of the material greatly affects the regime of the jet. In the liquid phase, dielectric materials undergo an extreme drop in viscosity and surface tension by orders of magnitude with temperature increase.^[52] In our case, we assume that a higher fluence leads to a higher temperature, hence higher jet speed, lower viscosity, and lower surface tension, therefore corresponding to a higher Weber number.

3.4. Third Regime: Wavy Nano-Pillars

The third regime corresponds to the nano-pillars shown in **Figure 2g–i**. This regime is nearly stochastic and appears for fluences above 3.5 (a.u.). As a consequence of the extremely high sensitivity to processing parameters, the shot-to-shot reproducibility varies between 0 and $\approx 70\%$. In this regime, we can ob-

serve either the absence of any kind of structures except a crater (**Figure 2g**), or the presence of a small structure (**Figure 2h**), or even very high nano-pillars reaching 15 μm in height (see **Figure 2i**). All the pillars in this regime present very wavy morphology compared to the previous regimes. The comparison of their morphology with water jets is striking as shown in **Figure 6**. The dripping regime shape corresponds to the small pillar shown in **Figure 2h**. This nano-pillar presents an elongated filament at the top, a sign of a probable generation of satellite droplets before solidification.^[53] The nano-pillar in **Figure 2i** can easily be associated with the Rayleigh regime.

To explain the third regime, we suppose that, at high fluences, the material inside the excited tube of material is in the liquid phase, with low viscosity, low surface tension, and under higher temperature and pressure than in the previous regimes.^[54] This condition leads to a more explosive ejection than in the other regimes, as suggested by the more significant cracks on the surface, which are much wider than the nano-pillar diameters (see the surfaces in **Figure 2g–i**). These conditions correspond to the hydrodynamics of liquid jets which undergo capillary instability as described above. Therefore, we understand our results with the following scenario: after material excitation and heating, an explosive phase occurs within the atomization regime. This phase is followed by the emission of a jet at a lower Weber number. The jet is perturbed by instabilities and then re-solidifies. The first explosive phase is probably the cause of the stochastic behavior in the third regime. The explosion can indeed easily modify the aperture on the surface, which plays the role of a nozzle, with obvious influence on the regime of the jet.^[55] We also remark that FIB milling reveals a void underneath the nano-pillar (**Figure 2k**), highlighting the extreme thermodynamics at play in this regime.

In the jet breakup theory, it is possible to calculate the wavelength of the main instability mode.^[56] This length depends on the physical parameters of the sapphire. In our case, the

calculated wavelength has a maximum at $\lambda = \pi d \sqrt{2 + 6 \sqrt{\frac{\rho v^2}{2d\sigma}}} \approx 6 \mu\text{m}$, where d is the jet diameter (700 nm), ρ the density (3030 kg m⁻³), ν the kinematic viscosity ($1.8 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$), and σ the surface tension (0.67 N m⁻¹), where this data correspond

to liquid sapphire at its melting temperature of 2323 K.^[45,53] It fits remarkably well with the period of 5 μm observed in Figure 2i.

We also remark that among all the results obtained, including those presented in subsequent sections, a maximal nanopillar height of $\approx 15\ \mu\text{m}$ has been reached many times in highly different conditions (energy, pulse duration, polarization, beam-sample relative position). This highlights the universality of the jetting process in the third regime again, as described by the capillary instability theory, which predicts a maximum of the breakup length, as we showed in Figure 6. The breakup length is the length over which the jet remains within a single segment of fluid. Above this maximal distance, the jet breaks up into droplets. The maximum height we found experimentally fits extremely well the theoretical formula of the breakup length $L = 0.5 d \sqrt{\frac{\rho}{\rho_a}} = 16.9\ \mu\text{m}$, where ρ_a is the density of air in our case.^[57] Since the maximal breakup length corresponds to the transition between capillary and shear instability ($We \approx \rho/\rho_a$ ^[57]), we can estimate that the maximum jet speed is of $\approx 800\ \text{m s}^{-1}$ within the same order of magnitude as shadowgraphy measurements of laser-induced forward transfer.^[58]

We also highlight that the cooling process is extremely fast since, in our experiment, the laser beam and the liquid sapphire jets are horizontal. We did not observe significant titling of the nano-pillars that could be attributed to gravity.

4. Influence of the Processing Parameters

In this section, we investigate the impact of the different processing parameters on the nano-pillar formation.

4.1. Fluence on the Sample Surface

In this subsection, we show that the nano-pillar formation process is mostly determined by the fluence of the main ring (doughnut) of the Bessel beam on the sample surface. In Figure S3, Supporting Information, we plot the evolution of the beam fluence of the main Bessel ring as a function of distance, and we have indicated the positions at which a nano-structure has emerged on the surface, for a fixed pulse energy of 6.1 μJ , together with the corresponding SEM images. It is apparent that for different positions, nano-pillars belonging to the three regimes mentioned above have emerged. We have repeated the experiment for different energies, and we have summarized our results in Figure S6, Supporting Information, where we report the height (top panel) and maximum diameter (lower panel) of the repeatable nanostructures (first and second regime) as a function of the main Bessel ring fluence on the sample exit surface. In the top panel, we also show the corresponding SEM pictures. The color marks the pulse energy.

We observe that the nano-structure average diameter remains nearly constant throughout our experiments, ranging from 800 nm to $\approx 1.2\ \mu\text{m}$. Besides, the height evolves quasi-linearly with the fluence. Most importantly, we can distinguish that the morphology of the nano-pillars changes for a fluence of ≈ 1.7 (a.u.). The third regime, with much less reproducibility, is reached for a fluence above 3.5 (a.u.).

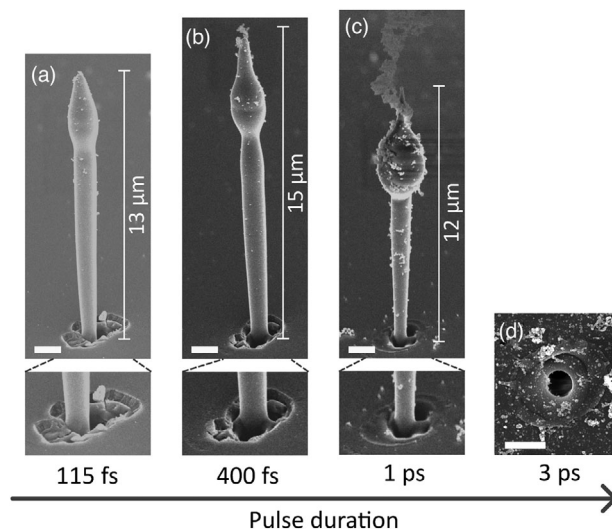


Figure 7. SEM images of laser-generated structures for different pulse durations. a–c) Pulse energy of 6.1 μJ and d) with a lower pulse energy of 5.3 μJ . Scale bars are 1 μm .

As we will see below, similar nano-pillars could be obtained for different processing conditions: azimuthal polarization, front surface processing, and pulse durations, for which we have repeated the same analysis (see next sections and Figures S4–S10, Supporting Information). The pulse energy and the position of the beam with respect to the surface both modify the deposited energy distribution and, therefore, the nano-pillar formation. Importantly, we remark in our data that the fluence of the main Bessel ring on the processed surface, shown in the horizontal axis in these figures, allows for distinguishing the regimes among the different pulse energies and positions used. It is, therefore, the important effective control parameter allowing us to classify our results. We can also see that the fluences corresponding to transitions are relatively close among the different pulse durations. These remarks hold for nearly all cases except for high pulse energy or long pulse duration. We identify the regimes using the SEM images and represent them using the colorbar between the two panels in each figure.

4.2. Pulse Duration

Pulse duration is an important parameter for the laser processing of dielectric materials. We compared four pulse widths (115 fs, 400 fs, 1 ps, and 3 ps). In the configurations we explored, we could obtain nano-pillars in each case except for 3 ps. The examples of the laser-generated structures are presented in Figure 7 for a pulse energy of 6.1 μJ (a–c) and 5.3 μJ (d). Increasing the pulse duration in the picosecond regime leads to nano-structures that apparently have all undergone transient liquefaction, corresponding to an absence of the first regime (we note that straight nano-pillars of the first regime were observed for 400 fs pulse duration). Stronger thermal effects are also apparent when examining the close-ups of Figure 7 (bottom row): at lower pulse duration (a) and (b), the crater at the surface is dominated by cracks while longer pulse duration (c) and (d) features molten material around the nano-pillar base. In most of the images, we

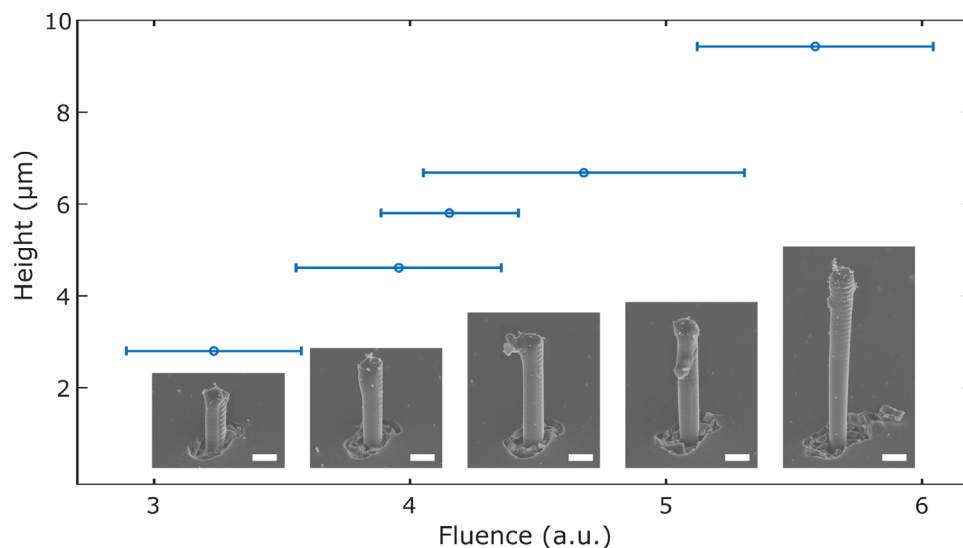


Figure 8. SEM images of nano-pillars obtained with azimuthal polarization with a pulse energy of 6.1 μJ. The graph shows the height as a function of the main Bessel ring fluence on the exit surface. Scale bars are 1 μm.

also notice the strong presence of small particles around and on the nano-pillars when increasing the pulse duration.

In particular, the case at 1 ps presents a structure at the top of the nano-pillars that very well matches the images of a jet of a molten metallic alloy in a liquid coolant in the atomization regime of reference.^[59] Our results for longer pulse durations can be understood as resulting from a first step of atomization followed by a jetting regime after the release of material through the surface and subsequent jet speed reduction. We note that the third regime with picosecond pulse durations is qualitatively less critical on position parameters than in the case of femtosecond pulse durations. We explain the overall differences between pulse durations as originating from lower pressure and temperature gradients for long pulse durations.

4.3. Polarization

As mentioned in the introduction, radial polarization highly enhances laser absorption via the resonance absorption mechanism. We repeated our experiments by switching the polarization state to azimuthal while maintaining all other parameters identical. A representative selection of results is shown in **Figure 8**. With the azimuthal polarization, even at high fluence, the nano-pillars remain straight and present the same periodic interference pattern as observed in **Figure 2b**, in the first regime. The highest nano-pillar we obtained is 9 μm high and 0.9 μm in diameter, leading to an aspect ratio of 10. We remark that the diameter of the nano-structures remains similar as in the case of radial polarization. As shown in **Figure 8**, the nano-pillar height evolves quasi-linearly with fluence, with a slope reduced by a factor 2 compared to the radial polarization. Our results highlight the difference in energy density deposition between radial and azimuthal polarizations: they show that the material irradiated with radial polarization reaches a higher temperature due to the resonance absorption,^[60] as it is the case in nu-

merical simulations of laser-surface interaction with Gaussian beams.^[61]

4.4. Front Surface Processing

We have also investigated the possibility of producing nano-pillars from the sapphire front surface. The tail of the beam was inserted in the sample, reproducing with symmetry the exit surface configuration (see **Figure 1**). Nano-pillars produced with radial polarization and pulse duration of 115 fs are shown in **Figure 9**. We show the highest pillar obtained across the different sample positions for each pulse energy. The morphology of the nano-pillars is consistent with the mechanism described above. For the lower energies, the nano-pillars are straight, and the height reaches 8 μm for an aspect ratio of 9 (diameter: 0.9 μm). We note that even at low fluence, the nano-pillars do not present the periodic pattern that we observed previously on the exit surface configurations: this supports the explanation of the interference between the beam and its reflection since it is not possible on the front surface configuration. At higher fluence, the capillary perturbations appear again, and the maximum height of nano-pillars observed is 15 μm, again in excellent agreement with the value predicted by the jet breakup theory (see **Section 3.4**). We can note the high presence of small particles that can be attributed to the surface damages caused by the outer rings of the Bessel beam and the probable occurrence of the atomization regime preceding nano-pillar formation.

4.5. Array Fabrication

Nano-pillars hold significant relevance across various domains. Solar cells benefit from the incorporation of nano-pillars to enhance light absorption.^[62,63] In biology, nano-pillars find utility in areas such as cell adhesion studies and tissue engineering, facilitating interactions between cells and artificial substrates.^[64,65]

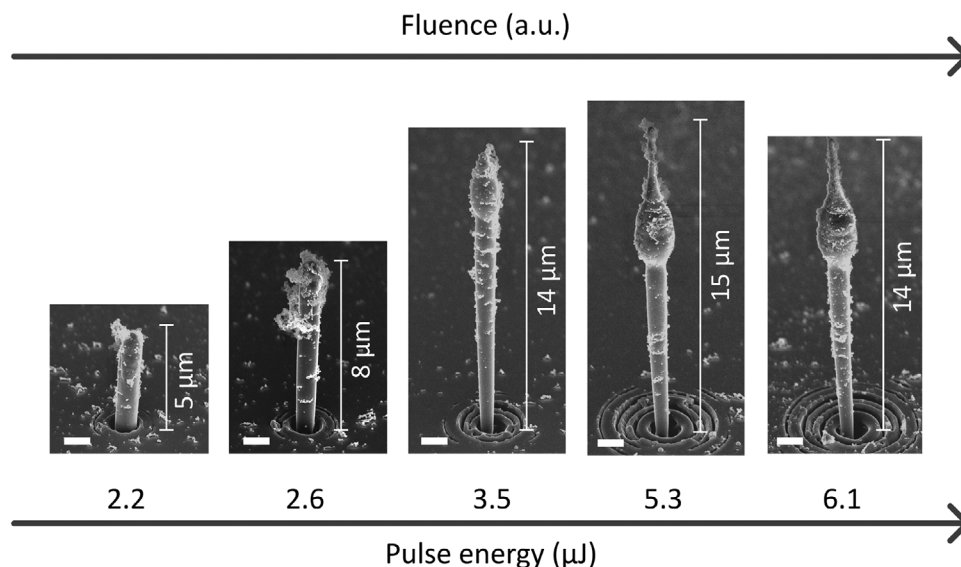


Figure 9. SEM images of the highest nano-pillars generated with front surface processing at different pulse energies and 115 fs pulses. Scale bars are 1 μm .

Moreover, in the realm of quantum electrodynamics, nano-pillars play a pivotal role in the manipulation of light-matter interactions, enabling the exploration of quantum phenomena.^[66] Additionally, nano-pillars find application as resonators, contributing to the development of highly efficient optical and electronic devices.^[67]

We have produced, as a proof-of-principle, periodic arrays of nano-pillars produced by sequential positioning and single-shot illumination. We believe that parallel processing could be identically performed. An example is shown in **Figure 10**. The minimal spacing for which the nano-pillars are homogeneous among the array is 7 μm . We remark it corresponds to the minimum separation distance for which an optical ray of the Bessel beam reaching the surface is blocked by a previously-inscribed 20 μm deep modification. We can therefore deduce that strong modifications are present deep within the bulk material underneath the nano-pillars.

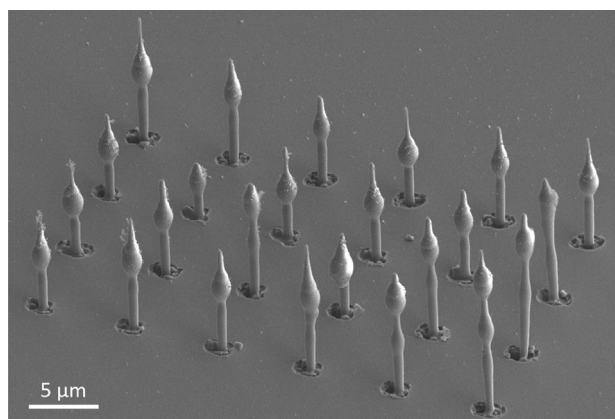


Figure 10. SEM picture of a matrix of nano-pillars with spacing of 7 μm (energy 6.1 μJ , pulse duration 115 fs and radial polarization).

5. Conclusion

We demonstrated for the first time the possibility of generating nano-pillars atop sapphire surface using a radially or azimuthally polarized first-order Bessel beam with a single ultrafast laser pulse. The nano-structures reach a height up to 15 μm with sub-micrometer diameter. Several morphologies could be observed with three main regimes. In a first approximation, the regimes can be controlled by the fluence of the Bessel beam on the exit surface. For the lowest fluences, straight nano-pillars are formed by the translation of solid material from the bulk. In the second regime, slick nano-pillars are formed by the extrusion of highly viscous molten sapphire. In the third regime, several morphologies of wavy nano-pillars could be observed and interpreted in the framework of the capillary instability theory of liquid jets of low viscosity. This theoretical framework very well predicts the period of the oscillations along the nano-pillar height, as well as the maximal nano-pillar height itself. Its universality has been observed among all the results we obtained with highly different laser pulse configurations.

Increasing the pulse duration reduces spatial gradients of temperature. Laser pulses with picosecond duration produce more thermally affected material while suppressing the first regime in which straight nano-pillars can be generated. The azimuthal polarization, for which the absorption is less intense, leads to less explosive conditions and favors this first regime.

Preliminary results, not reported here, show that similar results could be obtained within MgO crystal. They also indicate that the evolution of the fluence distribution along the beam propagation is highly influential in controlling the process: spatial distribution of laser-deposited energy density plays a key role in the mechanism of the nano-pillar formation. More studies are needed to fully decipher it. Specifically, next research should focus on evaluating the deposited energy density gradients and thermodynamic conditions to enable modeling of the overall nano-pillar generation process. Finally, we succeeded in

producing matrices of nano-pillars with 7 μm pitch. The main benefits of this nano-fabrication approach are its speed, absence of pre- or post-processing, and that it does not require clean-room facility. Our results open new perspectives in the field of laser-matter interaction and new material phase synthesis by compression. This fast nano-pillar fabrication approach will enable new applications in a number of different fields, such as metamaterials, mechanical components, nano-photonics, nano-phononics, or sensing.

6. Experimental Section

Experimental Setup: A Ti:sapphire laser with central wavelength at 800 nm was used. Thanks to a spatial light modulator and a 2f–2f system (relay lens and microscope objective Olympus MPLFLN x50), a Bessel beam with a cone angle of 36° in air was obtained at the sample position. To obtain a radial or azimuthal polarization, a radial polarizer converter (AR-Coptix, Switzerland) was inserted between the first lens and the microscope objective of the demagnification system. Because of the phase singularity imposed by the radial or azimuthal polarization distribution, the zero-order Bessel beam was transformed into a first-order one.

To observe both sample and beam, a 2f–2f system composed of a microscope objective (Olympus MPLFLN x50) and a relay lens was imaging the beam and the sample on a camera (Stingray F146B with 14 bits).

Beam Shape: The obtained Bessel beam was featured by a length in air of $\approx 20 \mu\text{m}$ (FWHM) and an angle of 36° , leading to a central ring of ≈ 800 nm diameter (considering the intensity maxima). Because of a singularity of the radial polarizer converter, a drop in the intensity profile was generated in the middle of the beam (see for the beam profile in Figure S1, Supporting Information). The pulse duration was checked using the autocorrelator PulseCheck 50 (APE, Germany) before the spatial light modulator. The dispersion induced by the rest of the optical setup is quasi-negligible.

Sample: The samples were sapphire c-cut with thickness $150 \mu\text{m}$. In the experiment, the sample was mounted on a precision 3-axis translation stage to allow the machining at different beam-sample positions. The sample was set on a motorized kinematic mount to ensure its orthogonality to the beam direction.

Experimental Procedure: The relative beam-sample position was changed over $30 \mu\text{m}$ around the peak of the beam by steps of $1 \mu\text{m}$. After the characterization of the beam and the alignment of the sample, six shots were repeated for each set of parameters with a distance of $25 \mu\text{m}$ between two consecutive shots. The regime is considered repeatable if at least five shots over six produce the same nano-pillar morphology within a height fluctuation of $\pm 1 \mu\text{m}$. It is possible that some nano-pillars could have been broken due to the sample handling between processing and SEM imaging, as nano-pillar-shaped structures were found on the surface of the sample.

Procedure for in-Bulk SEM Images: To obtain the images of the modifications inside the materials (see Figure 2), the region around the laser damage was milled with a focused ion beam (FEI Helios 600i). To avoid charging effects, a layer of chromium of ≈ 20 to 25 nm was deposited. To protect the interesting area from the direct interaction with the ion beam, a layer of $1 \mu\text{m}$ of platinum was deposited above. A milling procedure was performed with a nominal depth of $15 \mu\text{m}$ at a current of 21 nA to create a cuvette offering SEM imaging access, positioned $\approx 3 \mu\text{m}$ from the laser damage. In a second step, two cleaning cross-sections were performed: at 9 nA to approach the damage and subsequently at 2.5 nA to produce clean sections of the modified region. All the images were taken with an angle of 52° from the vertical.

Procedure for TEM Images: The TEM foils were prepared using a Thermo Fisher Scientific FEI 125 Helios Nanolab 600i FIB. The nano-pillar was protected with a thick carbon coating (Figure 4a) deposited on both sides and above the pillar before the milling and extraction of the foil. TEM characterizations were performed with a Cs-corrected TEM (NeoARM200F Cold FEG) operated at 200 kV . The instrument was equipped with a wide-angle energy dispersive X-ray spectrometer SDD CENTURIO-X from JEOL,

two scanning transmission electron microscope detectors (annular dark field and annular bright field from JEOL and Gatan) with a CMOS camera Gatan Rio ($4\text{k}\times 4\text{k}$), a CCD camera Ultrascan from Gatan ($2\text{k}\times 2\text{k}$), and an electron energy-loss spectrometer (EELS, Gatan GIF Quantum ERL).

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Author Contributions

V.V.B., M.H., R.G., L.F., and F.C. developed the setup. V.V.B. performed most of the data acquisition with the help of M.H. V.V.B. performed SEM imaging. V.V.B. and F.C. analyzed the experimental data. V.V.B. proposed the model, S.S.J. prepared the sample for TEM measurements, A.M.S.G. performed and interpreted TEM measurements. The manuscript was jointly written by V.V.B. and F.C. and revised by all authors.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

ultrafast laser, Bessel beam, nano-pillars

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